INTEGRATION OF OFF-RAMP AND ARTERIAL SIGNAL CONTROLS TO MINIMIZE THE RECURRENT CONGESTION ON THE I-495 CAPITAL BELTWAY

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Integration of Off-ramp and Arterial Signal Controls to Minimize the Recurrent Congestion on the I-495 Capital Beltway

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This study developed an integrated control model to contend with the impact of off-ramp queue spillback on both the freeway and arterials within the interchange control boundaries. The entire control system consists of two levels that compute the optimally coordinated signal strategies for intersections and off-ramps. Whereas the first level primarily handles oversaturated flows and blockage between lanes at congested intersections, the second level deals with the freeway mainline delays caused by the excessive off-ramp queue spillback; these components work together to produce the optimal systemwide signal and ramp control plans. In addition to developing control modules for oversaturated arterials and excessive off-ramp queues, the study also conducted experimental analyses using field data from the interchange between I-495 and Georgia Avenue. The experimental results indicate that, by accounting for how off-ramp queues impact delays of both freeway and arterial traffic, the integrated interchange control system can yield the best use of a roadway’s overall capacity and prevent the formation of freeway queues in the interchange area caused by the overflow of off-ramp traffic.
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Executive Summary

Effectively contending with the growing congestion on the Capital Beltway has long been the top priority and the most challenging task of transportation professionals in this region. Although a variety of factors has contributed to its deteriorating traffic conditions, insufficient freeway capacity to accommodate the ever-increasing demand from the Washington Metropolitan Area is certainly the top issue to address. Our extensive field observations of the congestion patterns on the Capital Beltway over recent years have revealed that many existing bottlenecks during peak hours are due to the spillback of the traffic queue from an off-ramp that often takes away the capacity of one to two mainline travel lanes when it exceeds the length of an auxiliary lane. Examples of bottlenecks caused by such off-ramp spillback vehicles can be found at the Connecticut Avenue and Georgia Avenue interchanges during peak hours.

Both field observations and simulation experiments conducted in this study further indicate: that (1) an interchange’s high off-ramp volume, in conjunction with the peak-hour arterial flow rates, will cause some intersection approaches to become oversaturated, consequently paralyzing traffic movements along the entire arterial; (2) an oversaturated arterial adjacent to the interchange can cause off-ramp queue lengths to extend beyond their auxiliary lanes and block the freeway’s mainline lanes; and (3) state-of-the-art signal optimization programs, such as TRANSYT-7F, cannot yield effective signal control plans for oversaturated arterials that often experience lane blockage between neighboring lanes and queue spillback to their upstream segments.

In view of those identified critical issues, this study focused on developing an integrated off-ramp and arterial signal control system for urban interchange that can dynamically adjust the signal plan to minimize the queue spillback from off-ramps to the freeway mainline while maximizing throughput on their neighboring arterials. The entire system consists of the following three primary components: (1) a real-time operational framework to effectively contend with the impact of off-ramp queue spillback on both the freeway and arterials within the interchange control boundaries; (2) an arterial control model to optimize signalizing timings at all oversaturated intersections within the impact boundaries of a congested interchange; and (3) an integrated interchange control model to
minimize the total freeway and arterial delay if any off-ramp queue has spilled back to the freeway mainline.

An extensive evaluation conducted in this study using both the field data and various experimental scenarios convincingly indicates that the proposed system framework with its embedded control models is capable of capturing interactions between turning and through traffic flows, as well as congestion propagation between neighboring intersections. It can effectively prevent the formation of local bottlenecks caused by queue spillback or lane blockage. Further analysis of the traffic queue patterns also shows that, by accounting for how off-ramp queues impact delays of both freeway and arterial traffic, the interchange optimal control system can yield the best use of a roadway’s overall capacity and prevent the formation of freeway queues in the interchange area caused by the overflow of off-ramp traffic. Hence, the integrated control model developed from this study can potentially serve as an effective tool for responsible highway agencies to exercise the proper level of control, based on the detected distribution of ramp queue length, and traffic volumes on the freeway as well as arterials.
CHAPTER 1: INTRODUCTION

1.1 Research Background

Effectively contending with the growing congestion on the Capital Beltway has long been the top priority and the most challenging task of transportation professionals in this region. Although a variety of factors has contributed to its deteriorating traffic conditions, the insufficient capacity of the freeway mainline to accommodate the ever-increasing demand from the Washington Metropolitan Area is certainly the top issue to address. Our extensive field observations of the congestion patterns on the Capital Beltway over recent years have revealed that many existing bottlenecks during peak hours are due to the spillback of the traffic queue from an off-ramp that often takes away the capacity of one to two mainline travel lanes when it exceeds the length of an auxiliary lane. Examples of bottlenecks caused by such off-ramp spillback vehicles can be found at the Connecticut Avenue and Georgia Avenue interchanges during peak hours. Thus, while policy makers explore demand-side methods, such as congestion pricing and HOT lanes, it is essential that the potentially cost-effective and near-term deployable strategy of integrated off-ramp control be investigated.

Thus, this study developed a control system for the integrated operation of off-ramps and their local arterial signals with two layers of operational objectives. The first layer involves implementing a monitoring mechanism that can prevent off-ramp vehicles from spilling back into the mainline, thereby reducing its capacity. The second layer applies optimal control theory to maximize the throughput of the target roadway segment, including both the off-ramp and its upstream and downstream intersections. Depending on traffic conditions and the available capacity of the target local arterial, one shall investigate the impacts of assigning different priorities to the off-ramp vehicles on the arterial traffic progression and flow speed, if the off-ramp queue has been controlled within the auxiliary lane.

It should be mentioned that traffic bottlenecks caused by off-ramp spillback queues are quite common congestion patterns on many metropolitan beltways. Neither research institutions nor operational agencies have yet developed effective strategies to contend with their impacts on freeway mainline capacity.
1.2 Research Objectives and Project Scope

To meet its primary objective, this study focused on developing an integrated off-ramp and arterial signal control system for urban interchange that can adjust the signal plan to minimize the queue spillback from off-ramps to the freeway mainline while maximizing throughput on neighboring arterials. The proposed system contained three principal components: (1) a real-time operational framework to effectively contend with the impact of off-ramp queue spillback on both the freeway and arterials within the interchange control boundaries; (2) an arterial control model to optimize signalizing timings at all oversaturated intersections within the impact boundaries of a congested interchange; and (3) an integrated interchange control model to minimize the total freeway and arterial delay if any off-ramp queue has spilled back to the freeway mainline.

Unlike most existing models on interchange traffic control, the focus of this research was on the scenario in which traffic volumes on both the freeway and its local arterial are high enough to cause intersection overflow and off-ramp spillback to the freeway mainline segment. Hence, the development of control algorithms to optimize the overall operational efficiency for such congested interchanges needs to consider the tradeoff between freeway and arterial traffic delays, while also accounting for potential lane blockages at local intersections due to oversaturated traffic conditions during different control periods.

Note that, since most target interchanges on the I-495 Capital Beltway consist of several on- and off-ramps and intersections, it is essential to ensure that implementing the optimal systemwide control will not cause undesirable local consequences, such as increasing the left-turn queue length at a particular intersection. Thus, the scope of this study also included a comprehensive sensitivity analysis of all possible traffic scenarios, based on field data from the interchange of I-495 and George Avenue, and the selection of operational constraints for each control point at the overall system optimization process.

1.3 Report Organization

To take advantage of existing studies on this vital issue, this study began with an extensive literature review of the available interchange and corridor control models. The findings are presented in Chapter 2. Since signal design and ramp operational strategies
are the two principal components of an integrated interchange control system, this chapter also summarizes some state-of-the-art developments associated with both vital research issues.

Chapter 3 presents the overall framework for the proposed integrated system control, including the interrelationships between all principal components, the operational flowchart, and potential extensions to a corridor-level control.

Chapter 4 details the arterial control component, which functions to generate the set of time-varying optimal timing plans for each signal within the control boundaries during the congested peak hours. It includes an analysis of the complex interrelations between the signal phasing plan and the distribution of traffic volumes and formulations for traffic blockages between lanes under spillback conditions. This chapter also focuses on illustrating the modeling methodology used to integrate traffic conditions at all intersections and ramps in an operational optimal control structure.

Chapter 5 illustrates the advanced interchange control system, which includes the proposed arterial component, but further considers the potential impacts of off-ramp queue spillback on the freeway through traffic. This chapter focuses on formulations of the freeway mainline traffic delay and its interdependent relationships with the traffic volume on the local arterials. The chapter also looks at how to select the proper control objective for the target interchange system under various congestion levels and how best to use the resulting measures of effectiveness (MOE).

Chapter 6 reports the evaluation results with respect to the proposed integrated control system using the field data from the interchange between I-495 (the Capital Beltway) and Georgia Avenue. This chapter also analyzes the essential subject of how best to use the computed optimal results for systemwide control operations without yielding unacceptable levels of service at any local control junctions.

Chapter 7 summarizes the primary research findings from this study, including valuable lessons obtained from developing all primary models and evaluating the integrated control system with field data. Concluding comments, along with potential operational issues that may emerge in any future system implementation, are also the main focus of this chapter.
CHAPTER 2: LITERATURE REVIEW

2.1 Introduction

To take best advantage of existing studies on freeway control and interchange traffic management, the research team extensively reviewed the related literature covering integrated interchange control, ramp metering, and signal optimization. Critical issues and technical constraints identified from the literature review task actually served as the basis for finalizing the research objectives and scope of this study.

This chapter is organized as follows: Section 2.2 presents state-of-the-art models for interchange control, including strategies for both freeway ramps and their neighboring arterial signals. Section 2.3 reviews integrated models for corridor control, as their core modeling methods are all applicable for use in contending with queue formation and dissipation around a congested interchange. Section 2.4 summarizes existing studies for freeway access control, including both on- and off-ramps, which are often the locations that become the bottlenecks. Section 2.5 and section 2.6 highlight the strengths and deficiencies of the literature on arterial signal optimization, especially regarding effectively tackling traffic flows at an oversaturated intersection.

2.2 Integrated Interchange Control Strategies

Integrated interchange control refers to controlling the interchange signals and on-ramp meters in an integrated manner. Many researchers over the past several decades have worked on this problem, and some have converted their research results into commercial products (Munjal, 1971; Messer and Berry, 1975; Messer, Fambro et al., 1977; Radwan and Hatton, 1990; Dorothy, Maleck et al., 1998; Chlewicki, 2003). For instance, Venglar et al. (1998) developed PASSER III, a computer program designed to analyze the operation of an isolated interchange. Engelbrecht and Barnes (2003) investigated eight possible controller features to improve the operational efficiency of diamond interchanges under moderate traffic conditions. However, most early studies on this subject focused only on undersaturated conditions, not congested scenarios where queue spillback may take place at either an off- or on-ramp and the overflow blockage between lanes may occur at neighboring intersections.
More recently, Kovvali et al. (2002) began to address the issue of optimizing the control for congested interchanges and proposed an extension to PASSER III with a GA (genetic algorithm)-based model which can optimize the diamond interchange signals for both undersaturated and oversaturated traffic conditions with link queue spillback. The core logic of their proposed method involved employing the delay equations in the Highway Capacity Manual (HCM) and the platoon dispersion model in TRANSYT-7F to capture the dynamic interrelationships between the spatial evolution of traffic flows and the resulting delay under different signal plans.

Building on the work by Kovvali, some researchers (Tian and Messer et al., 2004) tackled the on-ramp spillback problem using an integrated model that concurrently optimized on-ramp metering and interchange signal control parameters. Further, Lee and Messer et al. (2006) conducted field investigation of the performance of actuated controls used at diamond interchanges under congested conditions.

Along the same lines, Fang and Elefteriadou (2006) developed a different solution algorithm with a forward dynamic programming method that was adaptive in nature and thus responsive to fluctuating traffic demand evolving from moderate to congested conditions. Li and Chang et al. (2009) designed an real-time operational system framework to prevent off-ramp queues from spilling back to the freeway mainline segment by controlling the adjacent arterial signals. Zhang, et al. (2009) attempted to use a local synchronization control scheme for the same type of congested interchange. Their core control logic is to manage the queues at critical locations by coordinating traffic signals at neighboring intersections and freeway on-ramp meters. The model formulations for network traffic dynamics are represented with the traditional cell transmission concept.

In summary, although recent studies on the subject of interchange control have started to address complex interactions between congested traffic flows and the resulting on-ramp queues, many vital issues arising during oversaturated conditions remain to be tackled, such as overflow blockage between through and turning vehicles on local arterials and the spillback of off-ramp queues impeding freeway mainline traffic.
Integrated Corridor Control Model

Integrated corridor control refers to the concurrent optimization of freeway ramp flows and signal timing plans on adjacent arterials so as to maximize the throughput of the entire system. Since an interchange is a subsystem of a traffic corridor, many modeling concepts or creative algorithms proposed in the literature for these two traffic control types share the same potential for applications. Thus, this section also briefly reviews related modeling strategies in the literature for integrated corridor control.

Most existing studies of corridor control fall into one of the two following categories: (1) heuristic methods, along with simulation analysis for feedback adjustment control strategies; and (2) mathematical formulations with traffic flow and control theories. Some early studies using heuristic methods include the control process proposed by Reiss (1981) and Van Aerde and Yagar (1988), both of which rely on simulation programs to evaluate the effectiveness of the proposed methods and to make necessary adjustments. Another study of the same type, conducted by Pooran and Sumner (1996), identified four types of coordination strategies and sixteen types of control tactics for managing corridor traffic.

In the second category, Cremer and Schoof (1989) were the first researchers to formulate an integrated corridor control model that included off-ramp traffic diversion, on-ramp metering, mainline speed limit control, and signal timing plans on the surface streets. They modeled freeway traffic dynamics with the classical continuous flow model and the arterial flow evolution with the platoon dispersion model from TRANSYT. The proposed solution algorithm is a mixed-integer nonlinear optimal control model along with a heuristic decomposition approach. Van Den Berg et al. (2004) proposed a model predictive control (MPC) approach for mixed urban and freeway traffic in urban corridors, based on enhanced macroscopic traffic flow formulations. Their study represents freeway dynamics with a continuous flow model, and reflects the horizontal and destination-dependent queues on urban arterials with a study by Kashani and Saridis (1983). Their model has the overall control objective of minimizing the total system travel time.

Grounded on a similar core theory, but with different formulations for traffic flow interactions between successive control segments, Chang et al. (1993) presented a dynamic system-optimal control model for a commuting corridor consisting of a freeway.
and a parallel arterial. Their proposed formulations integrated ramp metering control with arterial signal optimization under the common functional objective of minimizing the total corridor travel time, and solved all control parameters concurrently with a linear approximation algorithm.

Focusing mainly on nonrecurrent congestion in commuting corridors, Wu and Chang (1999) later formulated a linear programming model with a heuristic algorithm to solve for the optimal ramp metering rate, the off-ramp diversion percentage, and arterial signal timing plans. Their proposed methodology employs classical traffic flow conservation relationships to capture the temporal and spatial evolution of vehicle flows on each segment of the freeway and arterial, including the flow transition between roadway segments and the flow discharge at intersections. To improve the computing speed for a large corridor network, this study further investigated a two-regime approximation for the nonlinear speed-density relationship that allows the application of a specially designed successive linear programming algorithm to solve the systemwide optimal state.

Along the same line of research, Papageorgiou (1995) developed a similar model to address corridor traffic management but used classical optimal control theory to model the traffic flow dynamics and the store-and-forward recursive relationship to reflect the feedback interrelations between the observed traffic conditions and the responsive adjustment of the control strategies. Tian and Balke (2002) analyzed the effectiveness of the integrated operation of surface street and freeway systems with VISSIM, a micro-simulation model, and concluded the potential benefits with integrated control at the corridor level. More recently, Tian (2007) formulated an integrated ramp metering model for diamond interchange control system based on the computed total delay occurring on the freeway mainline and its ramps, with a second-by-second analysis of the arriving and departure flow rates.

Overall, the existing studies of corridor congestion management have reported the necessity and effectiveness of integrating freeway access control with local arterial signal timing plans. Researchers working on this subject also share common concerns about the inevitable tradeoff between model accuracy and computing efficiency. Thus, how to formulate an integrated corridor control model that is sufficiently reliable and efficient for real-time applications remains a challenging on-going issue for the community.
2.4 Freeway Access Control Strategies

Most studies of freeway access control focus on developing various on-ramp control strategies, which aim to keep the downstream freeway volume under the roadway capacity by limiting its on-ramp volume. Based on the employed logic, one can divide existing ramp metering studies into the following two categories: pretimed and automated metering control. Studies of the former sort use historical average volumes to compute the ramp metering rate, whereas those in the latter category focus on keeping traffic conditions near prespecified levels based on real-time traffic measurements. The automated metering strategies can use either actuated or adoptive control models, depending on the employed algorithm and the available data.

One pioneering study that used the linear programming method to produce the pretimed ramp metering rate was by Wattleworth (1963). The core idea of this study was to compute the volume on each freeway mainline segment using the historical average upstream volume and then to determine the on-ramp metering rate, with the control objective of maximizing the total entering flow rate within the freeway capacity constraints. Papageorgiou (1980) extended the same basic concept on formulating the interrelations between ramp flows and mainline flows with the linear programming method that incorporated a constant travel time for each freeway segment and produced the optimal metering rate with a decomposition approach. Similar studies along this line, but with different objective functions, are also available in the literature (Yuan and Kreer; Tabac, 1972; Wang, 1972; Wang and May, 1973; Chen, Cruz et al., 1974; Chen, Cruz et al., 1974; Schwartz and Tan, 1977).

Note that pretimed ramp metering strategies aim to optimize ramp metering rates under stable traffic patterns. Hence, they often lead to underutilization of the freeway mainline capacity under time-varying traffic conditions.

In view of the deficiencies inherent to all pretimed metering strategies, some researchers have proposed the use of automated metering strategies to optimize metering rates based on real-time measured traffic volumes and occupancies. Most of such studies belong to one of the following categories: (1) local responsive control, where the ramp metering rate is determined solely by mainline traffic volumes on the adjacent freeway; and (2) coordinated ramp metering control, which computes the set of time-varying
metering rates for ramps within the control boundaries, based on the detected systemwide traffic conditions.

Some early studies in the former category include the demand-capacity strategy by Masher, Ross et al. (1975); the zone-based control strategies by Stephanedes (1994); Xin, and Michalopoulos et al. (2004); and the congested pattern control approach by Kerner (2005). The demand-capacity strategy attempts to fully utilize the downstream capacity of the freeway mainline by reducing the ramp flow to its minimum level if the downstream occupancy exceeds the critical level. This control algorithm follows an open-loop disturbance-rejection policy and is quite sensitive to disturbances caused by either traffic or measurement errors.

The zone-based control strategy, employed by the Minnesota DOT for many years, seeks to maintain a target level of traffic volume within each freeway zone, defined as a segment containing only one ramp. This strategy’s effectiveness varies with the accuracy of the estimates for all associated control parameters, including the number of divided zones, the estimated bottleneck capacity, and the entering and leaving volumes of each zone over the control period. Xin et al. (2004) later extended this algorithm to stratified ramp control, which considers both the ramp demand and its queue size. The congested pattern control approach by Kerner (2005) employs a three-phase traffic flow concept to keep the on-ramp bottleneck at the minimum possible level that will not propagate its congestion patterns to upstream segments.

The occupancy-based control strategy determines the ramp metering rate based on the occupancy of the downstream freeway mainline, using feedback regulation to maintain a prespecified occupancy. Examples of occupancy-based strategies include ALINEA (Papageorgiou, Hadj-Salem et al., 1991), the neural control algorithm (Zhang and Ritchie, 1997; Xin, Michalopoulos et al., 2004), and the iterative-learning approach (Hou, Xu et al., 2008). The ALINEA algorithm proposed by Papageorgiou et al. (Papageorgiou, Hadj-Salem et al., 1991) is a closed-loop ramp metering strategy that uses classical feedback theory and dynamically adjusts the metering rates in response to detected differences between the target and measured occupancies. The local artificial neural network model attempted by Zhang and Ritchie (1997) employs a multilayer feed-forward control structure, based on the fundamental diagram of traffic flow theory. Both ALINEA and neural control algorithms are reasonably effective for moderate congestion.
but not for heavy congestion where queue spillback may occur. The core concept of the iterative-learning approach (Hou, Xu et al., 2008) is to formulate the density-based ramp metering control as an output-tracking and disturbance-rejection problem; this approach then employs an iterative learning algorithm along with the error-feedback method to yield a robust metering rate.

In view of the myopic nature of local control, some researchers have devoted tremendous efforts over the past decades to various coordinated metering strategies, including cooperative ramp metering, competitive ramp metering, and integrated ramp metering. An extensive summary of these strategies can be found elsewhere (Jacobson, et al., 1989; Nihan, 1991; Bogenberger, 1999; Zhang, et al., 2001). The literature includes some field experiments and extensive simulations of such strategies (Bogenberger, 1999).

The main control objective of a cooperative ramp metering system is to prevent the formation of both freeway mainline congestion and ramp spillback by adjusting the metering rate based on local traffic conditions and information about the spatial distribution of traffic volume over the entire system. The helper ramp metering algorithm by Lipp et al. (1991), which belongs to this category, consists of a local traffic-responsive metering algorithm and a centralized, coordinated operational override feature. The local responsive algorithm selects one of six predefined metering rates, based on each on-ramp’s upstream mainline occupancy. If a meter rate reaches its critical status, the coordinated control begins to exercise its override function. The linked-ramp algorithm (Banks, 1993), another example in the same category, is based on the demand-capacity concept and uses the upstream volume to determine the local metering rate.

Unlike the cooperative metering models, the core logic of competitive algorithms involves computing two sets of metering rates based on both local and systemwide conditions and then selecting the more restrictive one to implement. The bottleneck algorithm (Jacobson, Henry et al., 1989) and the systemwide adaptive ramp metering model (SWARM) (Paesani, Kerr et al., 1997; Ahn, Bertini et al., 2007) are two such studies in this category.

The bottleneck algorithm uses upstream occupancy data and bottleneck data to determine the metering rate for both a local ramp and the freeway bottleneck, and then selects the more restrictive one. At the local level, it employs historical data to approximate the volume-occupancy relationships around capacity for each ramp. The
local rate is set to be the difference between the estimated capacity and the measured upstream volume. To obtain the bottleneck metering rate, the algorithm first identifies bottlenecks and its volume reduction with the classical traffic flow theory, and then computes the bottleneck metering rate by distributing the reduced volume to upstream ramps with prespecified weights.

The \textit{SWARM algorithm} also operates at two control levels. The local level computes the metering rate based on the local density and its systemwide reduction from ramps upstream of a critical bottleneck and then uses predetermined weights to distribute the volume to the upstream ramps. The algorithm identifies the bottlenecks based on the predicted, rather than measured, traffic conditions. Integrated ramp metering control directly generates metering rates from systemwide information. \textit{METALINE}, the fuzzy local algorithm, and the coordinated artificial neural network algorithm belong to this category.

\textit{METALINE} (Papageorgiou, 1990), an extension of ALINEA, is theoretically sound, but finding the proper control parameter matrices and the target occupancy vector is difficult. \textit{Fuzzy logic algorithms} (Sasaki and Akiyama, 1986; Chen, May et al., 1990; Meldrum and Taylor, 1995; Taylor, Meldrum et al., 1998) convert empirical knowledge about ramp control into fuzzy rules. The effectiveness of such control algorithms depends on the accuracy of the embedded fuzzy rules derived from empirical data. The \textit{coordinated artificial neural network algorithm} (Wei and Wu, 1996) divides the freeway segment under control into several zones and computes the metering rate based on the collected volume-to-capacity ratios upstream and downstream of the ramp and the queue length within each zone.

One common feature of all adaptive ramp metering algorithms is that they explicitly specify an objective function, such as minimizing total travel time, maximizing system throughput, etc., to govern the selection of metering rates for all ramps within the control boundaries. The \textit{Hanshin algorithm} by Yoshino et al. (1995) pioneered the use of such algorithms. They employed a linear programming model to maximize the total number of vehicles entering the system while preventing traffic congestion in any segment of the expressway and the surrounding road networks. Lovell and Daganzo (2000) proposed an improved time-dependent control strategy for freeway networks with bottlenecks and a computationally efficient greedy heuristic algorithm for solving the
metering rate. Recognizing the complexity of model formulations and the difficulty in obtaining real-time OD information, Zhang and Levinson (2004) formulated a similar linear program that uses only variables directly measurable from detectors. Gomes and Horowitz (2006) also presented a similar linear control model, but used the asymmetric cell transmission method (ACTM) to minimize the total freeway travel time.

The *dynamic metering control algorithm* by Chen et al. (1997) represents another cluster of studies. This algorithm generally consists of four operational elements: state estimation, OD prediction, local metering control, and area-wide metering control. At their core, such algorithms form a hierarchical structure with a local feedback control module (ALINEA) and a systemwide control model. The latter employs a linear-quadratic feedback control to produce nominal metering for local controllers, which then compensate the nominal set of metering rates based on the detected local traffic disturbances and prediction errors.

The *linear-quadratic (LQ) feedback control algorithm* is one of the most commonly studied methods within the automatic control theory for coordinated freeway ramp metering (Yuan and Kreer, 1971; Kaya, 1972; Papageorgiou, 1983; Payne, Brown et al., 1985; Papageorgiou, Blosseville et al., 1990). The key logic of such LQ feedback strategies is to convert the nonlinear traffic state equations around a certain desirable trajectory, employing a quadratic penalty function in the objective function to represent the state and control deviations from the desired trajectory.

The *successive optimization algorithm* represents another school of methods for solving the ramp metering rates for large-scale networks. Chang et al. (1994) presented such an algorithm to solve the complex control model that captures the dynamic evolution of traffic with a two-segment linear flow-density relationship. An example of such a model with a rolling time horizon for freeway corridors can be found in the literature (Wu and Chang, 1999).

In summary, ramp metering is one of the most direct and efficient means to mitigate freeway local congestion if appropriately implemented. The benefits include an increase in freeway mainline throughput and a reduction in travel time or delay. However, these are achieved at the cost of excessive on-ramp queues, which may spill back and block neighboring urban arterials (Levinson and Zhang, 2006). To achieve
better performance for the entire corridor, the control boundaries should include both the freeway and its neighboring arterials.

### 2.5 Arterial Traffic Signal Control Strategies

Signal control is an essential control strategy used to increase arterial capacity and to mitigate daily congestion. Webster and Cobbe (1967) first introduced a formula to optimize the signal timing plans for an isolated intersection. Building on Webster’s work, some researchers later proposed pretimed signal control models that employed phase-based strategies to optimize the splits, cycle length, and phasing in order to minimize the total delay. Examples of such studies are SIGSET (Allsop, 1971) and SIGCAP (Allsop, 1976). SIGSET applied Webster’s nonlinear total delay function for undersaturated conditions (1958) as the objective function and imposed some linear constraints on key control parameters. SIGCAP is mainly used to minimize delay for multiple demand patterns under the same constraints. A similar model, but using the binary-mixed-integer programming method, also appeared later in the literature (Improta and Cantarella, 1984).

Some researchers have extended the core concept of SIGCAP to formulate a so-called reserve capacity model (Wong and Yang, 1997; Wong, Wong et al., 2007).

All of the aforementioned example models are used only to control undersaturated, isolated intersections, neglecting the interrelationships of traffic flow evolution between intersections. Hence, optimizing the progression of all intersections in the same arterial emerged as a popular research subject (Morgan and Little, 1964). One pioneering study by Little et al. (1966; 1981) following this line of inquiry proposed the use of mixed-integer linear programming. Their model, named MAXBAND, aimed to provide the optimal set of offsets for all signals on the same arterial so as to maximize its inbound and outbound progression bandwidths. This mixed-integer linear programming model was solved with the traditional branch-and-bound algorithm; later, Chaudhary et al. improved its efficiency (1991). Several researchers later extended this pioneering arterial model to multiband phasing plans, including optimizing the left-turn phase sequence (Chang et al., 1988), the weighted bandwidth for each directional road section (Gartner et al., 1991; 1996), and the time-varying demand conditions (Han, 1996).

Instead of maximizing the progression band, TRANSYT (Robertson, 1969) offered an alternative signal control objective of minimizing a performance index consisting of prespecified MOEs, such as delay, number of stops, or queue length. This
signal design software is one of the most popular programs among both the research and application communities, and its results are often used as the baseline for evaluating various new signal control strategies (Papageorgiou, Diakaki et al., 2003). The core logic of TRANSYT was used later in a responsive signal network control system, SCOOT (Split, Cycle, Offset Optimization Technique) by Hunt et al. (1982).

Note that, due to the emergence of new sensor technologies and to the necessity of responding to traffic conditions in real time, the focus of traffic control researchers has evolved from optimizing pretimed arterial signals to developing real-time adaptive or semi-adaptive systems. Some popular real-time signal control systems include: SCAT (Sims and Dobinson, 1980), OPAC (Gartner, 1983), PRODYN (Henry, Farges et al., 1984), CRONOS (Boillot, Blosseville et al., 1992), RHODES (Sen and Head, 1997), and ARTC (Kim, Liu et al., 1993). The advent of intelligent transportation systems has turned the design and implementation of these real-time control systems into a popular task. Their effectiveness in contending with saturated traffic conditions and the resulting costs and benefits, however, remain on-going research issues.

2.6 Signal Control Models for Oversaturated Conditions

Oversaturation refers to conditions where traffic queues persist from one cycle to the next, due either to insufficient green splits or to lane-blockage. In such conditions, traffic queues along signalized arterials may block upstream intersections, thus exacerbating already congested conditions. Gazis et al. (1963) were the pioneer researchers who employed a graphic method to optimize two closely spaced and oversaturated intersections.

In 1997, Abu-Lebdeh and Benekohal (1997) developed an algorithm to optimize the signal timing for oversaturated arterials with a queue polygon approach, which assumed the existence of a continuous queue and a link blockage. They later extended their proposed GA-based solution to include a disutility function for evaluating a variety of traffic management scenarios (Abu-Lebdeh and Benekohal, 2000, 2003). Along the same lines, Abu-Lebdeh, et al. (2007) further developed several models that could capture the interactions of traffic streams between neighboring lanes and among successive signals under oversaturated traffic demand levels.

In the same vein, Chang and Lin (2000) analyzed queue evolution at an isolated intersection cycle by cycle, based on the assumptions of a constant arrival rate and the
continuous formation of the traffic queue. Their study employed two objective functions: one, in a quadratic form, was for the delay of each cycle during the entire oversaturated period; the other, a performance index, accounted for the total delay and stop penalty. Chang and Sun (2004) later extended this model to optimize an oversaturated signalized network.

Hadi and Wallace (1995) proposed an enhancement function to TRANSYT-7F that could optimize signal-timing plans under congested conditions. TRANSYT-7F, Release 8 (Li and Gan, 1999), also offers a function to model link spillback and lane blockage by reducing the corresponding link saturation flow. For the same oversaturated intersection, Park, Messer et al. (1999) employed the queue polygon method to compute the queue delay and to track the link blockage by continually checking the end-of-queue vehicle. They presented both a preliminary and an enhanced solution algorithms for signal control at congested intersections based on the core logic of GAs (Park, Messer et al., 2000).
CHAPTER 3: OVERALL SYSTEM FRAMEWORK

3.1 Introduction

This chapter presents the overall structure of the proposed integrated off-ramp control system for managing recurrent congestion under various traffic conditions. This chapter also illustrates the interrelationships between its principle components, along with critical control factors and underlying assumptions.

The remaining sections of this chapter are organized as follows: Section 3.2 presents the major research issues and challenges involved in developing a system capable of contending with recurrent congestion at urban freeway interchanges, including off-ramp overflow, on-ramp queue spillback, and intersection lane blockage. Section 3.3 illustrates the control flowchart of the proposed integrated control system, based on the research scope and intended applications. Finally, Section 3.4 discusses the proposed functions for each principle control component and their operational interrelationships.

3.2 Key Research Issues

The proposed system aims to maximize the operational efficiency of congested urban interchanges. Given the research objectives and the required system functions stated in Chapter 1, the development of such a system must first address the following major research issues:

- How to capture the interactions of traffic patterns that include lane and link blockages as they evolve from moderate congestion to oversaturated conditions;
- How to model the complex interrelationships between traffic queues on on-ramps, off-ramps, and freeway mainline segments at various congestion levels.
- How to balance the delays between freeway and arterial vehicles to achieve the optimal state for the entire system;
- How to formulate all of the identified complex interactions between both freeway ramp and arterial traffic flows and their evolving patterns with an integrated signal-ramp control model that can yield effective and reliable solutions for real-time applications; and
— How to contend with the occurrence of traffic measurement errors and still yield robust solutions for field operations.

To handle the above issues, the research team divided the entire study into the following tasks:

Task 1: Modeling the interrelationships between the off-ramp queue and lane blockages at neighboring intersections, as well as on-ramp spillback at various congestion levels. This task focused on contending with recurrent congestion patterns in which saturated local traffic conditions may cause the formation of off-ramp queues without affecting the operational capacity of the mainline segment.

Task 2: Formulating an integrated interchange control model that can account for the trade-off between delays on local arterials and the freeway mainline, yielding optimal systemwide congestion control. The proposed model is expected to concurrently optimize the on-ramp and off-ramp metering plans, as well as signal timing plans for the adjacent local arterials.

Task 3: Developing a generalized interchange control model to contend with recurrent or nonrecurrent congestion scenarios where off-ramp queue may spill back into the freeway mainline and interfere with the merging traffic flow from one or more upstream ramps. This task tackled the severe congestion pattern where both the freeway and local arterial are oversaturated and the off-ramp queue may significantly reduce the mainline capacity, spilling back to upstream ramps.

Task 4: Designing efficient solution algorithms for both the base model for off-ramp control and the extended model for integrated interchange system optimization. The algorithm needs to be capable of generating efficient control parameters in response to information deficiencies and dynamic traffic flow interactions between the freeway and arterials at various congestion levels.

Task 5: Evaluating the effectiveness of the proposed system and its embedded models with extensive numerical experiments and field tests. The primary focus of this task was to ensure the applicability of the developed system to the target I-495 interchange, which often experiences off-ramp queue spillback during daily commuting hours. Extensive numerical experiments were used, along with traffic scenarios observed in the field, to assess the potential and constraints of implementing the integrated control system under various traffic conditions.
3.3 System Control Structure and Key modules

To ensure that the results from each of the above tasks can be integrated into a seamless control structure and can be activated based on the detected congestion level, this study developed an overall control architecture for the proposed system with the following three levels:

Level 1: The off-ramp queue spills back to the freeway mainline. The control action for such a scenario will consider the mainline traffic delay in optimizing the signal timings at the off-ramp and intersections on the neighboring arterial.

Level 2: The on-ramp queue spills back to its upstream intersection. Note that insufficient metering rate may cause the queue vehicles to block one or more arterial through lane(s), consequently causing the through traffic to spill back to upstream intersections if the arterial through demand is larger than its remaining capacity. The control strategy at this level will activate its oversaturated intersection module to maximize the total throughput within the control boundaries.

Level 3: The freeway mainline in the interchange area experiences a moving queue and spills back to the upstream interchange. This level of control is designed for congested scenarios where both freeway and local arterial volumes at the interchange have reached the saturation level. The on-ramp queue has spilled back to nearby arterial through lanes, and the off-ramp vehicles have propagated to the freeway mainline lanes and to an upstream on-ramp.

Due to the need to investigate the driver compliance behavior given multiple detour routes in the Level-3 congested scenario, the study excluded its control strategy development from the research scope, and focused on resolving all complex modeling issues in Level-1 and Level-2 scenarios. Future field implementation results of the level-1 and level-2 control strategies can serve as the basis for developing the Level-3 control methods.
Input

Off-ramp spillback?

Yes → Model 4: Integrated multi-interchange control (not included in this research)

No → Model 3: Integrated single interchange control

No → Model 2: Integrated off-ramp control

Yes → Model 1: Integrated on-ramp control

On-ramp spillback?

Yes → Freeway Mainline Spillback to upstream?

No → Model 3: Integrated single interchange control

No → Do nothing

On-ramp spillback?

Yes → Model 1: Integrated on-ramp control

No → Model 2: Integrated off-ramp control

Figure 3-1 System Control Flowchart

Figure 3-1 illustrates the feedback process for the proposed integrated interchange control operations, which takes traffic demand and the existing signal timings as inputs and then executes the simulation model to check whether or not queue spillback is occurring at on- and off-ramps.

On-ramp metering and arterial signals (including off-ramp signals) will be operated independently if neither experiences any queue spillback. If queue spillback occurs only at off-ramps, the system will execute the off-ramp integrated control model to maximize system performance. Likewise, if only on-ramps exhibit excessive queues, the proposed system should activate just the on-ramp control model to balance freeway and arterial delays. All modules in the proposed integrated system will be activated if both on-ramps and off-ramps are suffering from long queue spillbacks. The simulation
module also needs to check freeway mainline spillback and then execute the multi-
interchange model to coordinate all control plans activated at the two neighboring
interchanges.

Note that the entire system illustrated in Figure 3-2 requires various inputs for its
online operations, including

- Roadway geometric features, such as the number of ramps, the distance
  between ramps and intersections, and the lengths of the left-turn bay, the
deceleration lane, and the on-ramp acceleration lane;
- Traffic volumes on the freeway’s mainline and ramps, as well as on the
  arterials and their intersections;
- Turning proportions at both neighboring intersections and off-ramps;
- Operational constraints for signal timing and metering plans; and
- Traffic flow parameters that reflect local driving characteristics.

To provide the aforementioned operational functions in response to various levels
of saturated and oversaturated traffic congestion, the proposed integrated interchange
control system has the following modules: an arterial signal timing optimization module,
an off-ramp integrated control module, an on-ramp integrated control module, a single-
interchange integrated control module, and an extended interchange control module. The
interrelationships between those modules are illustrated in Figure 3-2.

Note that the arterial signal timing module aims to optimize the cycle length,
offset, and green split for all signals within the control boundaries under both under- and
oversaturated conditions. The proposed module has the capability to take into account the
blockage between lanes and spillback between intersections.

The off-ramp integrated control module will incorporate ramp queue delay and its
impact on freeway mainline traffic into the arterial signal timing module to ensure the
proper balance between these two roadway systems. The on-ramp integrated control
module extends the functions of the local arterial signal optimization module and
concurrently account for on-ramp flow delays in the systemwide signal control process.
All of the aforementioned modules with a prespecified overall control objective naturally
form the single-interchange integrated operational module.
The single interchange control system can be extended to cover multiple interchanges if the freeway queue, due to both heavy mainline volume and off-ramp spillback, reaches upstream on-ramps. Effectively controlling such congestion patterns, however, is a much more complex problem. The performance of the entire traffic system must be maximized from the corridor management perspective, and potential detour routes might also require identification to balance the traffic volume between the primary commuting freeway and alternative routes. Since the compliance of drivers with control strategies and guidance information is one of the most critical issues determining the effectiveness of corridor-level operational strategies, this study cannot cover this level of development and will leave such an extension for a future project.

Figure 3-2 Key System Modules
CHAPTER 4: ARTERIAL TRAFFIC FLOW AND SIGNAL MODELS

4.1 Introduction

This chapter presents the methodology for modeling the complex traffic flow interactions between intersections and the potential blockage between neighboring lanes due to oversaturated demand. Its focus is on formulations for signal optimization and the control process under different congestion levels. Since queue spillback and its resulting blockage to through movements often occur on local arterials receiving off-ramp flows from congested interchanges, the model formulations detailed in this chapter offer the foundation for developing an integrated arterial signal optimization system that can take full account of the channelization effects on turning traffic and also capture the movement blockage between lanes.

The remaining sections of this chapter are organized as follows: Section 4.2 will discuss the modeling methodology for arterial traffic dynamics under oversaturated traffic conditions. Section 4.3 will focus on the signal optimization model and its solution algorithm developed with the commonly-used Generic-Algorithm (GA). Section 4.4 will report the conclusions.

4.2 Modeling Traffic Flow Interactions at Signalized Intersections

To model the temporal and spatial interactions of traffic flows at a signalized intersection, one can conceptually divide each link into the following four zones: the merging, propagation, diverging and departure zones (see Figure 4-1). Vehicles entering such a link will move over these four zones and then bound to their respective destinations. Notably, vehicles for left-turn and through movements could block each other due to spillback if the bay length and signal timings are not adequate for the time-varying traffic volume. The traffic queue caused by lane-blockage could spill back to upstream intersections under oversaturated traffic conditions.
To optimize the signal plans for arterials experiencing lane-blockage conditions at some intersections, the research team employed the Cell Transmission concept (CTM) by Daganzo (1994, 1995b) to formulate the flow interactions in the above four zones. CTM is a finite difference approximation of the traffic flow model by Lighthill and Whitham (1955) and Richards (Richards 1956). Its core concept is to divide the target roadway into a number of homogeneous sections (named cells), and each has its length equal to the distance traveled by a vehicle at the free-flow speed during one unit time interval.

Any model developed with CTM can track the states of the traffic system at any time instant by the number of vehicles in each cell, denoted as $n_i^t$. In addition, CTM employs the following commonly-used parameters in representing the key traffic flow variables, where time $t$ represents the time interval $[t, t + 1]$:

- $N_i^t$ is the buffer capacity, defined as the maximum number of vehicles that can be presented in cell $i$ at time $t$, which is the product of cell length multiplied by the jam density;
- $Q_i^t$ is the flow capacity in time $t$, defined as the maximum number of vehicles that can flow into cell $i$, which is the product of the cell’s saturated flow multiplied by the length of time interval;
- $y_{ij}^t$ defines the number of vehicles leaving cell $i$ and entering cell $j$ at time $t$.

Any CTM model generally consists of three types of cells: the ordinary cell, the merging cell, and the diverging cell. The ordinary cell can have only one upstream and
one downstream cells; the merging cell has multiple upstream cells but one downstream cell; the diverging cell can have only one upstream cell but multiple downstream cells. The following two expressions illustrate the recursive relationships between these three types of cell:

\[ n_i^{t+1} = n_i^t + y_{i,in}^t + y_{i,out}^t \]  
(4-1)

\[ y_{i,in}^t = \sum_{k \in R(i)} y_{ki}^t \text{ and } y_{i,out}^t = \sum_{j \in R^-(i)} y_{ij}^t \]  
(4-2)

Equation (4-1) represents the flow conservation relationship at the cell level, which means that the number of vehicles within a cell in the next time interval equals the vehicle number of this interval and the difference between all entering and departing vehicles. The second and third terms in Equation (4-1) vary with the cell category, where \( y_{ij}^t \) needs to be computed with a traffic flow-density relationship.

To represent the complex traffic behavior such as lane-blockage, it is necessary to track the vehicle number for each movement. Thus, this study employs the following recursive relationship at the movement level for each cell, in additional to the flow conservation at the cell level:

\[ n_{i,m}^{t+1} = n_{i,m}^t + y_{i,m,in}^t - y_{i,m,out}^t \]  
(4-3)

where \( n_{i,m}^t \) is the vehicle number for movement \( m \) of Cell \( i \); \( y_{i,m,in}^t \) is the number of those vehicles that travel from upstream cell (i.e., Cell \( s \)) to Cell \( i \) and will stay in the movement \( m \) of Cell \( i \); and \( y_{i,m,out}^t \) is the number of vehicles that depart from movement \( m \) of Cell \( i \).

4.2.1  Merging zone

In the merging zone, vehicles from different upstream approaches will join together to form a new traffic stream. During oversaturated traffic conditions, the large volume of vehicles from this aggregate traffic stream could cause long queue spillback and thus block the upstream traffic as shown in Figure 4-2.
The merging cell is best suited for modeling the traffic flow interactions in the merging zone. As illustrated in Figure 4-3, Cell-C represents the merging zone; Cell-A, Cell-B, Cell-D represent the upstream through, right-turn, and left-turn approaches. At signalized intersections, since upstream vehicles will be given different priorities to enter the merging zone based on the signal phasing plan, one can then use Equations (4-4) to capture their relationships.
\[ y_{ic}^t = \min\{n_i^t, Q_i^t, \delta [N_c - n_c^t]\}, i = A, B, D \quad (4-4) \]

Where \( \delta = 1 \), if \( n_i^t \leq Q_i^t \), and \( \delta = \frac{w}{v} \), if \( n_i^t > Q_i^t \), in which \( w \) represents the backward propagating speed of the disturbances and \( v \) is the free-flow speed. When the merging zone represented by Cell-C is full (i.e., the vehicle number in Cell-C, \( n_c^t \), equal its buffer capacity, \( N_c^t \)), no vehicle can enter the merging zone (i.e., \( N_c^t - n_c^t = 0 \) which implies \( y_{ic}^t = 0 \)).

Hence, with the given turning percentage from each movement, one can update the number of vehicles for each movement during each time interval with the following expression:

\[ y_{c,m,in}^t = r_{lm}^t \left( \sum_i y_{ic}^t \right), i = A, B, D \text{ for each movement } m \quad (4-5) \]

Where \( r_{lm}^t \) denotes the percentage of vehicles joining each movement; \( l, m \) represent the link identity number and movement, respectively.

**4.2.2 Propagation zone**

In the propagation zone, the interactions between vehicles increase with the traffic volume. From the aggregate perspective, the flow-density relationship can best represent such interactions. Hence, to compute the optimal signal plan for an arterial, one needs to realistically formulate the temporal and spatial relations of vehicles evolving over the link between neighboring intersections.
To tackle this issue, this study employs the ordinary cell to capture this type of vehicle interactions in the propagation zone. As illustrated in Figure 4-4, the number of cells in the propagation zone may vary with the link length. Each ordinary cell has one upstream cell and one downstream cell. Equation 4-6 computes the number of vehicles exiting cell $i$ and entering cell $i+1$ in time $t$, $(y_{i,i+1}^t)$, a simplified flow-density relationship proposed by Daganzo (1956) to capture the traffic dynamics under various traffic conditions.

$$y_{i,i+1}^t = \min\{n_{i+1}^t, Q_{i+1}^t, \delta[N_{i+1} - n_{i+1}^t]\} \quad (4-6)$$

If one defines $S_i^t (= \min\{Q_i^t, n_i^t\})$ as the sending capacity, and $R_i^t (= \min\{Q_i^t, \delta(N_i^t - n_i^t)\})$ as the receiving capacity of cell $i$, then Equation (4-6) naturally evolves to Equation (4-7).

$$y_{i,i+1}^t = \min\{S_i^t, R_{i+1}^t\} \quad (4-7)$$

$$y_{i,m,\text{out}}^t = y_{i,\text{out}}^t \times \frac{n_{i,m}^t}{n_i^t} \text{ for each movement } m \quad (4-8)$$
4.2.3 Diverging zone – a new set of formulations

In the diverging zone, vehicles bound to different destinations may have to join different queues in order to be at their target movements. Hence, under oversaturated conditions, it is likely to incur blockage between different movements due to queue spillback in some movements. For instance, depending on the bay length and its incoming volume, the left-turn queue could spill back to block the through traffic.

Note that although there are several different types of lane blockage at an oversaturated intersection, the presentation hereafter will focus only on the formulations for interaction between left-turn and through vehicles. One can apply the identical concept to model all other types of blockage between lanes. Figure 4-5 and Figure 4-6 show two possible types of blockage between left-turn and through lanes at an intersection.

Figure 4-5 Left-turn vehicles block through traffic

Figure 4-6 Through vehicles block left-turn traffic
To realistically capture these two types of queue and lane blockage effect on neighboring movements, this study proposes a sub-cell modeling concept, an enhancement to the existing CTM methodology. Figure 4-7 illustrates the use of the proposed sub-cell concept to the diverging zone link that consists of a diverging cell, Cell i+1, which has two sub-cells: sub-cell L for left-turning vehicles and sub-cell T for through traffic.

**Figure 4-8 The sub-cell representation of a diverging signalized cell**
Figure 4-8 illustrates the use of three sub-zones to model the vehicle interactions in the diverging zone, where Zone 1, denoted by $N^t_1$, is the space exclusively for left-turn traffic; Zone 2, $N^t_2$, is the space only for through traffic; and Zone 3, $N^t_3$, is the space to share by left-turn and through traffic. Equations (4-9) and (4-10) presented below are for computing the buffer capacity of each sub-cell:

$$N^t_L = N^t_1 + N^t_3$$  \hspace{1cm} (4-9)

$$N^t_T = N^t_2 + N^t_3$$  \hspace{1cm} (4-10)

$$N^t_{i+1} = N^t_1 + N^t_2 + N^t_3$$  \hspace{1cm} (4-11)

Equation (4-11) captures the physical buffer capacity of diverging cell $i+1$. Note that one can divide these zones based on the channelization at the signalized approach. The buffer capacity of these sub cells explicitly reflects the turning bay effect. One can compute the flow capacity of each sub-cell, based on its number of lanes and the saturation flow rate.

Based on the above definitions, the study presents the following linear programming formulations to represent the time-varying status of such sub-cells:

$$\max \sum_m y^t_{i,m,out}$$  \hspace{1cm} (4-12)

$$\sum y^t_{i,m,out} \leq R^t_{i+1}$$  \hspace{1cm} (4-13)

$$y^t_{i,m,out} \leq \delta(N^t_{i,m} - n^t_{i+1,m})$$  \hspace{1cm} (4-14)

$$\sum y^t_{i,m,out} \leq S^t_i$$  \hspace{1cm} (4-15)

$$y^t_{i,m,out} \leq S^t_i \times \frac{n^t_{i,m}}{n^t_i}$$  \hspace{1cm} (4-16)

$$y^t_{i,m,out} \leq Q^t_{i,m}$$  \hspace{1cm} (4-17)

Equation (4-12) assumes that drivers always intend to fully utilize the available capacity and space. For instance, as shown in Figure 4-9, when the left-turn queue spillback occurs, the coming left-turn vehicles will inevitably occupy all the shared zone space if the volume continues to increase.
The new diverging model developed in this research can explicitly reflect the effect of the turning bay, and capture some lane blockage relations with Equations (4-12), (4-13), and (4-17). The third term in the parenthesis of Equation (4-12) is the minimum of these three terms, which implies \( w^t_i = \frac{R_L^t}{r^t_L} \). By substituting it into Equations (4-13) and (4-17), it leads to the following results: 
\[
y^t_{il} = R_L^t \quad \text{and} \quad y^t_{it} = R_L^t \times \frac{r^t_T}{r^t_L}.
\]
If \( R_L^t \) decreases, \( y^t_{il} \) and \( y^t_{it} \) will also decrease. When \( R_L^t = 0 \), it indicates that left-turn vehicles have blocked through traffic completely. In the scenario of through blocking left-turn traffic, one can perform the same analysis to formulate their relationships.

The segment in the departure zone is modeled with a signalized cell, and its flow capacity \( Q_i^t \) is defined as follows:
\[
Q_i^t = Q_{i,max} g_i^t \tag{4-18}
\]
where \( g_i^t \) is the green time in time interval \( t \).

### 4.2.4 An optimization model for oversaturated arterial signals

**Objective functions**

Depending on the traffic conditions, one can set the control objective function as maximizing the total system throughput or minimizing the total delay. Using the above formulations, this study has set the objective function of maximizing the system throughput as follows:

\[
Max \quad (Throughput = \sum_{t=0}^{T} \sum_{j \in s} \sum_{i \in \Gamma_j} y^t_{ij}) \tag{4-19}
\]
where $S$ is the sink cell set; $\Gamma^{-}(j)$ is the upstream cell set of cell $j$; and $T$ is total operating time period.

In CTM, the length of each cell is set to be the free-flow travel distance over a pre-specified unit, which means that the vehicles at each unit time in each cell can either stay or move to the downstream cells. Hence, one can approximate the delay as the difference between a vehicle’s actual and its free-flow travel times over a given distance. For instance, if some vehicles staying in the same cell over $n$ consecutive unit intervals, then it implies that they have experienced $n$ unit delay times.

More specifically, one can define the delay over each cell for time interval $t$ as $d_{i,t} = (n_{i,t-1} - \sum_{j \in \Gamma(i)} y_{ij,t}) \times \tau$, where $\Gamma(i)$ is the downstream cell set of cell $i$ and $\tau$ is the time period length. Thus, one can formulate an alternative objective function of minimizing the total system delay as follows:

$$
Min \left[ \text{total delay} = \tau \sum_{t=0}^{T} \sum_{i} (n_{i,t} - \sum_{j \in \Gamma(i)} y_{ij,t}) \right]
$$

As $\tau$ is a constant, the objective function of minimizing the system delay is identical to the follow expression:

$$
Min \left[ \text{total delay} = \sum_{t=0}^{T} \sum_{i} (n_{i,t} - \sum_{j \in \Gamma(i)} y_{ij,t}) \right]
$$

Signal timing operation

Figure 4-10 illustrates a typical four-leg intersection and the NEMA (National Electrical Manufacturers Association) eight-phase structure, where the right-turn on red is assumed to be permitted.

Using the NEMA phase system has two advantages: (1) it can model all possible phases for a signal by switching the sequence of some provided phases (see Figure 4-10); and (2) it offers the flexibility to accommodate exclusive left-turning traffic with the leading-lagging phases. Hence, through the sixteen NEMA phases, one can find the optimal one from all possible combinations of the candidate signal phasing plans.
Figure 4-10 NEMA eight-phase signal timing structure

The following equations illustrate the two-ring eight-phase structure:

\[ g_{k1} + g_{k2} = g_{k5} + g_{k6} \]  \hspace{1cm} (4-22)

\[ g_{k3} + g_{k4} = g_{k7} + g_{k8} \]  \hspace{1cm} (4-23)

\[ g_{k1} + g_{k2} + g_{k3} + g_{k4} = C_k \]  \hspace{1cm} (4-24)

\[ C_k = \frac{C}{2^{h_k}} \]  \hspace{1cm} (4-25)

\[ h_k = \begin{cases} 
1, & \text{signal } k \text{ has half common cycle length} \\
0, & \text{otherwise} 
\end{cases} \]  \hspace{1cm} (4-26)

\[ g_{kj} \geq MG_{kj}, j = 1, \ldots, 8 \]  \hspace{1cm} (4-27)

\[ MinC \leq C_k \leq MaxC \]  \hspace{1cm} (4-28)

\[ 0 \leq offset_k < C_k \]  \hspace{1cm} (4-29)

\[ g_{kj}, C_k, offset_k \text{ are integers} \]  \hspace{1cm} (4-30)

Where, \( g_{kj} \) is the green time for Phase j of signal k, \( C_k \) is the cycle length of signal k; \( MG_{kj} \) is the minimum green time of signal k at phase j; \( MinC \) is the minimum cycle length; \( MaxC \) is the maximum cycle length; \( C \) is the common signal cycle length; \( h_k \) is a binary variable that indicates whether signal k has a half common cycle length or not based the relation defined by Equation (4-26); and \( offset_k \) represents the offset of
signal k. Equations (4-22) and (4-23) indicate the existence of the signal barrier. Equations (4-24) and (4-25) enforce the cycle length constraints. Equation (4-27) confines the green time of each phase to be less than its minimal green time; and Equation (4-28) specifies a user-defined minimal and maximal cycle lengths. Equation (4-29) requires that the offset of signal k lie between 0 and its cycle length.

To compute the green time for each interval $t$ of the departure cell, it is essential to convert the green time of each phase as follows:

$$G_{k0} = G_{k4} = 0; \quad G_{ki} = \sum_{j=0}^{i-1} g_{kj}, \text{ for } i = 1, 2, 3 \quad (4-31)$$

$$G_{ki} = \sum_{j=4}^{i-1} g_{kj}, \text{ for } i = 5, 6, 7 \quad (4-32)$$

Where $G_{ki}$ is the total green time in the signal cycle illustrated in Figure 4-10.

### 4.3 Solution Algorithm

In the proposed system and its embedded models, the decision variables are the cycle length, green time split, and the offset of each signal. Due to the nature of those decision variables this study employed a Genetic-Algorithm (GA)-based solution method for the proposed model. GA is a search technique that has been successfully applied to optimize signal timings under various traffic conditions (Daganzo 1995b). To speed up the computing process of convergence, this study applied the elitist selection method to optimize all decision variables (Ceylan 2006; Ceylan and Bell 2004; Lo and Chow 2004; Park et al. 1999; Zhou et al. 2007).

The most critical part of developing a GA-based algorithm is to derive a good encoding scheme, i.e., how to represent possible solutions of the target problem by a gene series of 0-1 bits. This study employed an encoding scheme which includes the constraints (4-22) to (4-30), i.e., the signal timing decoded from the scheme will be feasible to constraints (4-22) to (4-30). The fraction-based decoding scheme, based on the NEMA phase’s structure proposed by Park, Messer et al. (1994) can satisfy all those
constraints except Equation (4-25). Hence, this study has grounded on their work, and extended its schema with the half common cycle length for certain signals.

\[
C = \text{MinC} + (\text{MaxC} - \text{MinC}) \times f_1
\]

\[C_k = C / 2^k\]

\[P_{k1} = \max(MG_{k1} + MG_{k2}, MG_{k5} + MG_{k6}) + \left[C_k - \max(MG_{k1} + MG_{k2}, MG_{k5} + MG_{k6}) - \max(MG_{k3} + MG_{k4}, MG_{k7} + MG_{k8})\right] \times f_2\]

\[g_{k1} = MG_{k1} + (P_{k1} - MG_{k1} - MG_{k2}) \times f_3\]

\[g_{k2} = P_{k1} - g_{k1}\]

\[g_{k3} = MG_{k2} + (P_{k2} - MG_{k2} - MG_{k3}) \times f_4\]

\[g_{k4} = P_{k2} - g_{k3}\]

\[g_{k5} = MG_{k5} + (P_{k1} - MG_{k5} - MG_{k6}) \times f_5\]

\[g_{k6} = P_{k1} - g_{k5}\]

\[g_{k7} = MG_{k7} + (P_{k2} - MG_{k7} - MG_{k8}) \times f_6\]

\[g_{k8} = P_{k2} - g_{k7}\]

\[\text{Offset}_k = C_k \times f_8\]

Figure 4-11 An enhanced fraction-based decoding scheme for signal design

A detailed description of the original scheme can be found in the literature. As illustrated in Figure 4-11, the proposed scheme sets the cycle length of signal \(k\) to half of a common cycle length if the half-cycle binary variable, \(I_k\), is 1. Otherwise, the cycle length is set to be the full common cycle length.

4.4 Conclusions

This study presented an enhanced Cell-Transmission Model for optimizing signal plans at intersections along a congested arterial. The proposed model with its innovative sub-cell modeling methodology is capable of capturing traffic flow interactions between neighboring lane groups due to queue spillback under high volume conditions. The arterial signal optimization model reported in the chapter can optimize the cycle length, split, and offset, under the presence of the link and lane group blockages.
CHAPTER 5: AN INTEGRATED INTERCHANGE CONTROL MODEL

5.1 Introduction

This chapter presents an integrated optimal control model that grounds on the arterial signal optimization model, but extends its formulations to capture the impact of off-ramp queue spillback to the freeway mainline at the interchange. The proposed interchange control model includes the freeway mainline traffic delays caused directly and indirectly by the moving queue at the off-ramp, and thus allows traffic engineers to assess the tradeoff between the freeway and its neighboring arterial delays under various traffic conditions.

Figure 5-1 illustrates a signalized interchange, which includes two closely spaced signals and two on- and two off-ramps. The distance between these two signals typically ranges from 500 ft in urban areas to 800 ft in suburbs. The short distance between these two intersections for receiving freeway traffic offers a very limited queue storage capacity, and thus often causes queue spillback between them under oversaturated conditions. For instance, insufficient signal timing for the off-ramp at intersection-2 may cause its queue to spill back to the rightmost lane of the freeway mainline segment, and consequently increase its lane-changing density in the traffic flow. Conversely, inadequate green duration for the arterial through traffic could create a link blockage between two intersections. Thus, it is essential to have an integrated control system that can best allocate the signal timings for all control points under various congestion levels from the perspective of the system optimization.
This chapter hereafter focuses on illustrating the formulation of a freeway model and its integration with the optimal arterial signal model presented in the previous chapter. The developed freeway traffic model aims to capture the following two types of complex traffic flow interrelationships: (1) the impacts of arterial traffic volume on the off-ramp queue length; and (2) the spillback of ramp queue vehicles on the delay and operational capacity of its neighboring freeway travel lanes.

The remaining sections of this chapter are organized as follows. Section 5.2 presents the core logic of the freeway traffic flow model. Section 5.3 illustrates the mathematical formulations for complex interactions between traffic flows and the model solution algorithm. Section 5.4 summarizes the concluding comments.

5.2 Modeling Methodology for Freeways

Figure 5-2 illustrates a typical freeway mainline that consists of two different segments, named Type-A and Type-B. Vehicles in the Type-A segment can head to either the downstream freeway mainline or the off-ramp, where all vehicles in the Type-B segment will move only to the downstream mainline segment.
To facilitate the formulations of the complex interactions between the freeway and ramp flows with the CTM methodology, this study first defines the following key parameters:

- **Time** $t$: the time interval $[t, t + 1]$:

- $n^t_i$: the number of vehicles in Cell $i$;

- $N_i^t$: the buffer capacity, defined as the maximum number of vehicles that can be in Cell $i$ at time $t$, which is the product of the cell length multiplied by the jam density;

- $Q^t_i$: the flow capacity in time $t$, and defined as the maximum number of vehicles that can move into Cell $i$;

- $y^t_{ij}$: the number of vehicles leaving cell $i$ and entering cell $j$ in time $t$.

---

**Type-A segment**: vehicles can go either to the downstream mainline segment or off-ramps.

**Type-B segment**: a mainline segment where vehicles can move only to the downstream mainline segment.

Figure 5-2 The freeway segments by destination

5.2.1 Modeling of Type-B Segments

Type-B segment contains one entry and one exit cells as shown in Figure 5-3. Such a segment does not include either an on-ramp or off-ramp. Equation (5-1) illustrates the relations for computing the number of vehicles that can exit from Cell $i$ and enter Cell $i + 1$ in time $t$, i.e., $y^t_{i,i+1}$. 

---

40
\[ y_{i,i+1}^t = \min\{n_i^t, Q_i^t, \delta[N_{i+1}^t - n_{i+1}^t]\} \quad (5-1) \]

Where \( \delta = 1 \), if \( n_i^t \leq Q_i^t \), and \( \delta = \frac{w}{v} \), if \( n_i^t > Q_i^t \), in which \( w \) represents the disturbances propagate backward speed, and \( v \) is the free-flow speed. Type-A is a two-stream section where vehicles in the traffic flow can come from either two origins or move toward two destinations.

Let \( S_i^t (= \min\{Q_i^t, n_i^t\}) \) be the sending capacity, and \( R_i^t = \min\{Q_i^t, \delta(N_i^t - n_i^t)\} \) as the receiving capacity of Cell \( i \), then one can rewrite Equation (5-1) as follows:

\[ y_{i,i+1}^t = \min\{S_i^t, R_{i+1}^t\} \quad (5-2) \]

*one-stream section: all vehicles have the same origin and destination (Type-B segment).
** two-stream section: vehicles in the traffic flow come from either two origins or move toward two destinations (Type-A segment).

**Figure 5-3 Modeling the traffic flow interactions in a Type-B segment by CTM**

Equation (5-3) represents the flow conservation relationship in the cell level, implying that the vehicle number of a cell in the next time interval equals the number of vehicles present in this interval and all entering vehicles but subtracting all leaving vehicles.
\[ n_{i}^{t+1} = n_{i}^{t} + y_{i-1,i}^{t} - y_{i,i+1}^{t} \]  

(5-3)

### 5.2.2 Modeling of Type-A Segments

To model Type-A freeway segment (see Figure 5-4), it is necessary to add one additional state variable, \( n_{E,i}^{t} \), and track the exiting number of vehicles with the following expression:

\[ y_{E,i,i+1}^{t} = \min \{ y_{E,i}^{t} \times \min \{ n_{i}^{t}, Q_{i}^{t}, \delta(N_{i+1} - n_{i+1}^{t}) \}, N_{E,i+1}^{t} - n_{E,i+1}^{t} \} \]  

(5-4)

Where \( y_{E,i,i+1}^{t} \) denotes the exit number of vehicles from Cell \( i \) to Cell \( i+1 \); \( r_{E,i}^{t} \) is the exiting percentage of vehicles in Cell \( i \) for time interval \( t \), which can be computed as \( r_{E,i}^{t} = n_{E,i}^{t}/n_{i}^{t} \); \( N_{E,i+1}^{t} \) is the buffer capacity for exiting traffic, i.e., the maximum number of exiting vehicles that can stay in cell \( i \).

![Figure 5-4 Modeling of the two-stream interaction in a Type-A segment by cell](image-url)

Equation (5-5) determines the total vehicle number from Cell \( i+1 \) to its downstream cell (Cell \( i \)). The underlying assumption is that the two different traffic streams are well mixed.

\[ n_{E,i}^{t+1} = n_{E,i}^{t} + y_{E,i-1,i}^{t} - y_{E,i,i+1}^{t} \]  

(5-6)
Equation (5-3) illustrates the flow conservation relationship within each two-stream cell. In addition, Equation (5-6) also represents the conservation law of the exiting flows if without queue.

![Figure 5-5 Type-A segment traffic dynamics](image)

As shown in Figure 5-5, one can further divide the Type-A segment into merging zone, propagation zone and diverging zone. Among these three zones, the propagation zone can be represented with the ordinary two-stream cells to capture the traffic dynamics. The modeling methodologies for merging zone and diverging zone are presented below.

**Merging zone**

As illustrated in Figure 5-6, one can use a merging cell (Cell C) to represent the merging zone, which consists of one entry cell for the upstream freeway segment and the other for the on-ramp. As the on-ramp traffic should yield to the freeway mainline flow, it is natural to determine the mainline entry volume \(y_{BC}^t\) first, and then the on-ramp entry volume after updating the merging cell vehicle number \(n_c^t\) by adding the entry vehicle number from the upstream freeway mainline cell \(y_{AC}^t\). Therefore, one can use Equations (5-7) and (5-8) to determine the entry flow from upstream freeway mainline and on-ramp.
\[ y_{AC}^t = \min\{n_{A}^t, Q_{A}^t, \delta[N_C - n_{C}^t]\} \quad (5-7) \]
\[ y_{BC}^t = \min\{n_{B}^t, Q_{B}^t, \delta[N_C - n_{C}^t - y_{AC}^t]\} \quad (5-8) \]
\[ y_{E, iC}^t = y_{iC}^t \times \xi_{E}^t, i = A, B \quad (5-9) \]

Where \(\xi_{E}^t\) is the predetermined exiting volume percentage of the downstream freeways segment at time interval \(t\).

**Figure 5-6 On-ramp traffic characteristics**

The entry capacity of on-ramp, \(Q_{B}^t\), is determined by the traffic dynamics in the merging zone as shown in Figure 5-6. The length of the acceleration lane and the traffic stream characteristics in the adjacent freeway lane are the two primary factors that may affect \(Q_{B}^t\). In this study, \(Q_{B}^t\) is determined with Equation (5-10).

\[ Q_{B}^t = (Q_{A}^t - y_{AC}^t) \times p_{C}^t \quad (5-10) \]

Where \(p_{C}^t\) is the vehicle proportion which is on the right-most lane at time interval \(t\). Equation (5-10) assumes that the on-ramp traffic could take all the remaining capacity of the right-most freeway lane.
**Diverging zone**

Under congested conditions, it is quite often that the off-ramp queue could spill back to the upstream freeway mainline, and occupy one or two through lanes. Also, the speed of the neighboring mainline lanes may also be reduced due to a high frequency of lane-changing maneuvers.

![Diagram of Diverging Zone](image)

**Figure 5-7 Exiting-queue effect in a diverging zone**

To reflect the impact of such complex flow interactions on the freeway mainline capacity, one can model the diverging zone with a diverging cell (named Cell A) and let its two downstream cells (Cell B and Cell C) represent the downstream off-ramp and freeway mainline segment, respectively (see Figure 5-8). The diverging zone under the proposed methodology consists of three sub-areas, denoted as TH, TE, and E. In sub-zone TH, all vehicles will head to the downstream mainline, whereas vehicles in sub-zone E will exit mainly to the adjacent off-ramp. In contrast, both through and exiting vehicles can share the space in sub-zone TE.

Figure 5-8 illustrates the concept of modeling each diverging cell with two sub-cells (Sub-cell TH and Sub-cell E) to represent its two different outgoing traffic streams. One can thus approximate the buffer capacity of Sub-cell TH, denoted as $N_{TH}^t$, with the equation $N_{TH}^t = N_1^t + N_2^t$. Likewise, the buffer capacity of Sub-cell E, denoted as $N_E^t$, is equal to the sum of $N_2^t + N_3^t$, where $N_1$, $N_2$ and $N_3$ are the maximum number of vehicles that can stay in each sub-zone.
Figure 5-8 Graphical illustration of the modeling concept for the diverging zone

\[ y = \min\{n_i^t, Q_i^t, \delta(N_A^t - n_A^t)\} \]  (5-11)

\[ y_{E,i,A}^t = \min\{yy_{E,i}^t, N_{E,A}^t - n_{E,A}^t\} \]  (5-12)

\[ y_{i,Th}^t = \min\{(1 - y_{E,i}^t) \times y, N_{Th}^t - n_{Th}^t\} \]  (5-13)

\[ y_{i,A}^t = y_{i,Th}^t + y_{E,i,A}^t \]  (5-14)

Where \( y \) is a temporary variable to simplify the description; \( y_{i,Th}^t \) stands for the vehicle number from cell \( i \) to the Sub-cell TH of cell A; \( y_{E,i,Th}^t \) denotes those vehicles which miss the off-ramp due to spillback. Equations (5-12) and (5-13) determine the total vehicle number from Cell \( i \) to the through sub cell of the diverging cell (Sub-cell TH of Cell A) and the exit sub cell (Sub-cell E of Cell A), which assumes that the two different traffic streams are well mixed. The exiting flows from the sub cells to its downstream cell follow Equations (5-15) and (5-16). Note that all those cells or sub-cells share the identical flow conservation relationships.
The saturated flow rate of the exiting sub-cell (sub-cell E) is clearly equal to the off-ramp saturated flow rate. However, computing the saturated flow rate for the through sub-cell (Sub-cell TH) is relatively complex. As mentioned previously, when the exiting queue from an off-ramp spills back to the freeway mainline, some length of mainline lanes neighboring to the off-ramp will become a slow-speed zone due to the rubbernecking and lane-changing effects. Equation 5-17 illustrates such an impact and the interrelationships between all contributing variables:

\[
Q_{TH}^t = Q_A \times \left(1 - \frac{L_{A,E}}{L_A}\right) \times \left[1 - \alpha_A \times \frac{n_{E,A}^t}{N_{E,A}^t}\right]
\] (5-17)

Where \( L_{A,E} \) is the number of lanes occupied by the exiting queue; \( L_A \) is total lane number of the freeway mainline; \( Q_A \times (1 - L_{A,E}/L_A) \) is the capacity of the unblocked through lane(s); \( \alpha_A \) is the maximal saturated flow deduction proportion, which is the reduced percentage of capacity when the exiting vehicles occupy all available buffer space of the freeway; \( n_{E,A}^t/N_{E,A}^t \) is the proportion of the exiting buffer capacity occupied by the exiting vehicles. Equation (5-17) assumes that the through saturated flow rate equals the capacity of remaining though lane(s) subjected to a reduction factor that increases with the exit queue length.

### 5.3 An integrated single-interchange control model

**Objective function**

Depending on the traffic conditions, one can set the control objective to maximize the total system throughput or minimize the total delay. With the above cell-based formulations, the objective function of maximizing the system throughput can be expressed as follows:

\[
Max \ (Throughput = \sum_{t=1}^{T} \sum_{j \in S} \sum_{i \in \Gamma^{-}(j)} y_{ij}^t)
\] (5-18)
Where $S$ is the sink cell set, $\Gamma^{-}(j)$ is the upstream cell set of cell $j$, and $T$ is total operating time period.

As mentioned in Chapter 4, the length of each cell is set to be the free-flow travel distance during a pre-specified time unit, which implies that vehicles in each cell can either stay or move to the downstream cells during each time interval. Hence, one can approximate the delay as the difference between a vehicle’s actual travel time and its free-flow travel time over a given travel distance. For instance, if some vehicles staying in the same cell over $n$ consecutive unit intervals, then it implies that they all have experienced the delay of $n$ unit times. More specifically, one can define the delay for each cell for time interval $t$ as $d^t_i = (n^t_i - \sum_{j \in \Gamma(i)} y^t_{ij})\tau$, where $\Gamma(i)$ is the downstream cell set of Cell $i$ and $\tau$ is the length of one time unit. The alternative objective function of minimizing the total system delay can be expressed as follows:

$$
\text{Min } \sum_{t=1}^{T} \sum_{i} \sum_{j \in \Gamma(i)} (n^t_i - y^t_{ij}) = \tau \sum_{t=1}^{T} \sum_{i} \sum_{j \in \Gamma(i)} (n^t_i - y^t_{ij})
$$

(5-19)

As $\tau$ is a constant, the minimal system delay objective function can further be stated as:

$$
\text{Min } Z = \sum_{t=1}^{T} \sum_{i} \sum_{j \in \Gamma(i)} (n^t_i - y^t_{ij})
$$

(5-20)

The formulations for signal control and the solution algorithm are identical to those presented in Chapter 4, except the inclusion of freeway related constraints.

### 5.4 Conclusions

This chapter presented an interchange integrated control model with the Cell-Transmission concept. The developed formulations reflect the complex interactions between ramp queue and mainline vehicles in the merging, propagation, and diverging zones at a typical freeway interchange. By integrating the arterial signal models with the freeway formulations, one can operate the ramp and signal control plan from the perspective of optimizing the efficiency of the entire interchange, including the tradeoff
between freeway and arterial delays. Due to the embedded relations for capturing the queue spillback impacts on neighboring traffic flow movements, the proposed interchange model is able to generate the optimal control strategies for oversaturated traffic conditions during congested peak commuting hours.
CHAPTER 6: EXPERIMENTAL ANALYSES

6.1 Introduction

This chapter presents the experimental results with the proposed arterial and off-ramp control models using field data from a congested interchange on the I-495 Capital Beltway. The performance evaluation first focuses on the delay and throughput of the entire arterial within the control boundaries, and then compares the tradeoff between freeway and arterial delays that take into account the ramp queue impacts on the freeway mainline traffic. To assess the effectiveness of all developed models, this chapter also presents their comparison results with TRANSYT-7F, one of the state-of-the-art software for arterial signal optimization.

The remaining sections of this chapter is organized as follows: Section 6.2 describes the target interchange on the I-495 Capital Beltway for experimental design, including its geometric features, traffic demand patterns, and selected measures of effectiveness (MOE) for performance comparison. Section 6.3 reports the evaluation results for the arterial signal optimization model and its performance comparison with TRANSYT-7F. Section 6.4 analyzes the effectiveness of the interchange control model for concurrent minimization of both the freeway and intersection delays within the control boundaries.

6.2 Experimental Design

Figure 6-1 shows the network configuration of the interchange between the Capital Beltway (I-495) and Georgia Avenue (MD97), including four signalized intersections from Forest Glen Road (MD192) to Seminary Road, and four major congested highway segments: I-495 Outer Loop (I-495 OL), I-495 Inner Loop (I-495 IL), MD 97 Southbound (MD 97 SB), and MD 97 Northbound (MD97 NB).
Parameters for the solution algorithm

All experimental scenarios in Table 6-1 employ the specially-designed GA algorithm to compute the parameters for the optimal systemwide control. Each experimental scenario also applies TRANSYT-7F (Release 10), one of the most advanced signal optimization programs for both research and practice, to generate the alternate set of control parameters. To be on the same basis for comparison, this study selected the same GA algorithm embedded in TRANSYT-7F to all experimental scenarios, and also used the same set of parameters such as 200 generations with a population size of 50, the crossover probability of 0.3, and a mutation probability of 0.01. The widely used corridor simulation program, CORSIM, was used to simulate all traffic scenarios listed in each experiment, and generated their MOEs under the optimal control strategies produced by TRANSYT-7F and the signal control model developed in this study.
6.3 Experimental Results of the Arterial Signal Optimization Model

Control boundaries

Figure 6-2 illustrates the control boundaries in each experimental scenario, which includes four intersection signals and two arterial segments of MD97 Southbound (SB) and MD97 Northbound (NB).

Figure 6-2 Control boundaries of the case study for arterial signal optimization

Traffic demand patterns

Table 6-1 summarizes the distribution of volume data for performing the numerical experiments and analyses, based on the day–to-day variation of field data from each entry and exit within the control boundaries. Note that the volume used in the experimental scenarios is increased at the rate of 10 percent from the low, medium, and high levels, based on the field data. Figure 6-2 shows each key location within the control boundaries.
Table 6-1 Demand scenarios for arterial signal optimization model (vehicle per hour)

<table>
<thead>
<tr>
<th>Entrance</th>
<th>Movements</th>
<th>Demand Scenario</th>
<th>Low</th>
<th>Medium*</th>
<th>High</th>
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<tr>
<td>A</td>
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<td>10,186</td>
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*The field-measured AM peak volume

Overall system performance comparison

Table 6-2 summarizes the MOEs of each experimental scenario under two candidate control strategies for the low, medium, and high demand scenarios defined in Table 6-1. All MOEs were the average of 50 simulation runs over the duration of one hour with CORSIM. The selected MOEs from simulation output include: network-wide total delay and system throughput. The results presented in Table 6-2 indicate that the arterial optimization model developed from this study outperforms TRANSYT-7F under all scenarios at the system level.
Table 6-2 Overall model performance comparison

<table>
<thead>
<tr>
<th>Demand Scenarios</th>
<th>Simulation Results from CORSIM (One hour)</th>
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<td>Total Throughput (vehicle)</td>
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<td>Total Throughput (vehicle)</td>
</tr>
<tr>
<td>High</td>
<td>Total Delay (vehicle-hour)</td>
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<tr>
<td></td>
<td>Total Throughput (vehicle)</td>
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</tbody>
</table>

* Delay improvement = TRANSYT-7F Delay – The Proposed Model Delay
Throughput improvement = The Proposed Model Throughput - TRANSYT-7F Throughput
Delay Improvement (%) = (TRANSYT-7F Delay – The Proposed Model Delay) / the Proposed Model Delay × 100%
Throughput Improvement (%) = (The Proposed Model Throughput - TRANSYT-7F Throughput) / TRANSYT-7F Throughput × 100%

C.I. = confidence interval

For example, at the high congestion level, the target set of arterial intersections with the signal optimization model yields a total delay of 259 vehicle-hours, about 39 percent less than if using TRANSYT-7F. The same range of improvement also exists at the low and medium volume levels as shown in Table 6-2. The 95% confidence intervals for each scenario also confirms that the improvements are statistically significant, and increase with the congestion level or the total volume entering the control boundaries. The overall results seem to imply that the proposed arterial model with its explicit consideration of queue spillback and lane-blockage due to overflow is especially applicable for optimizing signals under congested conditions.

Table 6-3 presents the delay incurred at those four intersections on MD 97 within the control boundaries. Based on the improvement at the local arterial, it is clear that the proposed signal control model, in comparison with TRANSYT-7F, can better redistribute the delays among all intersections, and significantly reduce the queue at the most congested location at the modest cost of other less congested intersections at the relatively low demand level. Similar redistribution patterns also exist among all intersections at the medium and high demand levels. As discussed previously, this is likely due to the fact that the signal control model takes into account the possible queue
spillback at all congested intersection approaches, and offers sufficient signal timings to accommodate such flow patterns that in turn prevent the queue formation and propagation to its upstream links.

At the arterial level, the signal control model yields a significantly lower total delay than TRANSYT-7F for MD 97 southbound (SB), a highly congested segment. The performance of these two models for MD 97 Northbound, however, are comparable because its volume is relatively low, and does not to cause any lane blockage or queue spillback.

In summary, the arterial signal optimization model developed from this study clearly outperforms the state-of-the-art program, TRANSYT-7F, at all different demand levels for the congested I-495/Georgia Avenue interchange, regardless of the total delay or system throughput. The mechanism embedded in the proposed model to capture the delay caused by blockage between lanes and queue spillback has proved its effectiveness in redistributing the delays from the most congested one to the remaining intersections, thereby minimizing the likelihood of having local bottlenecks at all demand levels.
Table 6-3 Total delay comparison by intersection (vehicle minutes)

<table>
<thead>
<tr>
<th>Demand Scenarios</th>
<th>Simulation Results from CORSIM (One hour)</th>
<th>The Proposed Model</th>
<th>TRANSYT-7F</th>
<th>Improvement*</th>
<th>Improvement* (%)</th>
<th>Improvement (95% confidence interval)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Low</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intersection 1</td>
<td>2242.41</td>
<td>6112.78</td>
<td>3870.37</td>
<td>63%</td>
<td>[5483.4, 2257.4]</td>
<td></td>
</tr>
<tr>
<td>Intersection 2</td>
<td>588.20</td>
<td>443.24</td>
<td>-144.95</td>
<td>-33%</td>
<td>[-109.1, -180.8]</td>
<td></td>
</tr>
<tr>
<td>Intersection 3</td>
<td>1815.50</td>
<td>1703.63</td>
<td>-111.87</td>
<td>-7%</td>
<td>[-32.1, -191.7]</td>
<td></td>
</tr>
<tr>
<td>Intersection 4</td>
<td>1235.07</td>
<td>1064.19</td>
<td>-170.88</td>
<td>-16%</td>
<td>[-67.5, -274.2]</td>
<td></td>
</tr>
<tr>
<td>MD 97 SB</td>
<td>3951.1</td>
<td>7207.9</td>
<td>3256.8</td>
<td>45%</td>
<td>[1668.9, 4844.7]</td>
<td></td>
</tr>
<tr>
<td>MD 97 NB</td>
<td>1475.1</td>
<td>1637.7</td>
<td>162.6</td>
<td>10%</td>
<td>[101.4, 223.7]</td>
<td></td>
</tr>
<tr>
<td><strong>Medium</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intersection 1</td>
<td>3771.26</td>
<td>9376.52</td>
<td>5605.26</td>
<td>60%</td>
<td>[7742.7, 3467.9]</td>
<td></td>
</tr>
<tr>
<td>Intersection 2</td>
<td>537.45</td>
<td>640.41</td>
<td>102.97</td>
<td>16%</td>
<td>[161.3, 44.6]</td>
<td></td>
</tr>
<tr>
<td>Intersection 3</td>
<td>1992.82</td>
<td>2183.95</td>
<td>191.13</td>
<td>9%</td>
<td>[277.0, 105.2]</td>
<td></td>
</tr>
<tr>
<td>Intersection 4</td>
<td>2318.74</td>
<td>1960.66</td>
<td>-358.09</td>
<td>-18%</td>
<td>[-221.3, -494.8]</td>
<td></td>
</tr>
<tr>
<td>MD 97 SB</td>
<td>4261.0</td>
<td>11943.5</td>
<td>7682.5</td>
<td>64%</td>
<td>[5843.2, 9521.8]</td>
<td></td>
</tr>
<tr>
<td>MD 97 NB</td>
<td>2011.0</td>
<td>2010.3</td>
<td>-0.7</td>
<td>-0%</td>
<td>[-84.7, 83.3]</td>
<td></td>
</tr>
<tr>
<td><strong>High</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Intersection 1</td>
<td>5967.06</td>
<td>16664.37</td>
<td>10697.31</td>
<td>64%</td>
<td>[12008.3, 9386.3]</td>
<td></td>
</tr>
<tr>
<td>Intersection 2</td>
<td>964.92</td>
<td>895.53</td>
<td>-69.39</td>
<td>-8%</td>
<td>[284.9, -423.7]</td>
<td></td>
</tr>
<tr>
<td>Intersection 3</td>
<td>2992.88</td>
<td>2779.33</td>
<td>-213.55</td>
<td>-8%</td>
<td>[57.8, -484.9]</td>
<td></td>
</tr>
<tr>
<td>Intersection 4</td>
<td>2689.92</td>
<td>2590.17</td>
<td>-99.75</td>
<td>-4%</td>
<td>[-8.0, -191.5]</td>
<td></td>
</tr>
<tr>
<td>MD 97 SB</td>
<td>6671.8</td>
<td>17109.8</td>
<td>10438.0</td>
<td>61%</td>
<td>[8845.1, 12031.0]</td>
<td></td>
</tr>
<tr>
<td>MD 97 NB</td>
<td>2854.6</td>
<td>2961.3</td>
<td>106.7</td>
<td>4%</td>
<td>[-73.4, 286.9]</td>
<td></td>
</tr>
</tbody>
</table>

* Delay improvement = TRANSYT-7F Delay – The Proposed Model Delay
Delay Improvement (%) = (TRANSYT-7F Delay – The Proposed Model Delay) / the Proposed Model Delay × 100%
C.I. = confidence Interval
6.4 Results of the Integrated Interchange Control Model

Control boundaries

Figure 6-3 illustrates the boundaries of the integrated interchange control model, including four arterial signals and two freeway segments (i.e., I-495WB and I-495EB).

Traffic demand patterns

Table 6-4 presents the volume for each control points based on the field data, and Table 6-5 defines the demand from Ramp-H for analyzing its impact on the overall system performance.
### Table 6-4 Basic demand for entrances and ramps (vehicle per hour)

<table>
<thead>
<tr>
<th>Entrance</th>
<th>Movements</th>
<th>Demand</th>
<th>Ramp</th>
<th>Movements</th>
<th>Demand</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Through</td>
<td>3,382</td>
<td>H</td>
<td>Right</td>
<td>670</td>
</tr>
<tr>
<td></td>
<td>Right</td>
<td>112</td>
<td></td>
<td>Left</td>
<td>930</td>
</tr>
<tr>
<td>B</td>
<td>Left</td>
<td>44</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Through</td>
<td>101</td>
<td>I</td>
<td>Enter</td>
<td>825</td>
</tr>
<tr>
<td></td>
<td>Right</td>
<td>179</td>
<td>J</td>
<td>Enter</td>
<td>1402</td>
</tr>
<tr>
<td>C</td>
<td>Left</td>
<td>596</td>
<td>K</td>
<td>Enter</td>
<td>829</td>
</tr>
<tr>
<td></td>
<td>Through</td>
<td>340</td>
<td>L</td>
<td>Exit</td>
<td>1179</td>
</tr>
<tr>
<td></td>
<td>Right</td>
<td>47</td>
<td>M</td>
<td>Exit</td>
<td>299</td>
</tr>
<tr>
<td>D</td>
<td>Through</td>
<td>7025</td>
<td>N</td>
<td>Enter</td>
<td>654</td>
</tr>
<tr>
<td>E</td>
<td>Through</td>
<td>6879</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>F</td>
<td>Left</td>
<td>553</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Right</td>
<td>25</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>G</td>
<td>Through</td>
<td>2,715</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>-----</td>
<td>21998</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### Table 6-5 Experimental scenarios (vehicle per hour)

<table>
<thead>
<tr>
<th>Entrance</th>
<th>Movements</th>
<th>Exit Volume Scenario (H Ramp)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Low</td>
</tr>
<tr>
<td>H</td>
<td>Right</td>
<td>586</td>
</tr>
<tr>
<td></td>
<td>Left</td>
<td>814</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>1400</td>
</tr>
</tbody>
</table>

### Table 6-6 Overall model performance comparison

<table>
<thead>
<tr>
<th>Demand Scenarios</th>
<th>MOEs</th>
<th>Simulation Results from CORSIM (One hour)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ICIC*</td>
<td>TY7F*</td>
</tr>
<tr>
<td>Low</td>
<td>Total Delay (vehicle-hour)</td>
<td>545.6</td>
</tr>
<tr>
<td></td>
<td>Total Throughput (vehicle)</td>
<td>20591</td>
</tr>
<tr>
<td>Medium</td>
<td>Total Delay (vehicle-hour)</td>
<td>542.8</td>
</tr>
<tr>
<td></td>
<td>Total Throughput (vehicle)</td>
<td>20735</td>
</tr>
<tr>
<td>High</td>
<td>Total Delay (vehicle-hour)</td>
<td>455.9</td>
</tr>
<tr>
<td></td>
<td>Total Throughput (vehicle)</td>
<td>20887</td>
</tr>
</tbody>
</table>

* ICIC: the proposed Interchange Integrated Control Model
* TY7F: TRANSYT-7F
* Delay improvement = TRANSYT-7F Delay – The Proposed Model Delay
* Throughput improvement = The Proposed Model Throughput - TRANSYT-7F Throughput
* Delay Improvement (%) = (TRANSYT-7F Delay – The Proposed Model Delay) / the Proposed Model Delay × 100%
Overall system performance comparison

Table 6-6 presents the network total delay over one hour with CORSIM under the control strategies produced by the integrated interchange model and TRANSYT-7F. As expected, the interchange optimization model outperforms TRANSYT-7F regarding the total delay at all three volume levels. The computed 95% confidence intervals also confirm that the improvements are statistically significant, and increase with the congestion level.

With respect to throughput, the integrated interchange model yields a comparable level of performance with TRANSYT-7F under the low volume scenario. This is understandable because the system throughput generally equals its total demand if without congestion, regardless of the implemented control strategies. However, as the volume increases and congestion may occur, then whether an implemented control model is effective or not will impact significantly on the resulting throughput. This is evidenced by the better performance of the presented model in comparison with TRANSYT-7F at the moderate and high demand levels.

Note that the total system delay under the control strategies by the interchange optimization model actually decreases with an increase in the Ramp-H volume. Table 6-7 presents the total delays on both the freeway and arterial segments within the control boundaries under three different volume levels. The results indicate that this optimization model can yield the comparable level of freeway delay (16312 vs. 16091 vehicle-minutes) but far less arterials delay (16426 vs. 20931 vehicle-minutes) than with TRANSYT-7F under the low demand level.

The improvements become much more pronounced if the traffic volume exiting from off-ramp-H increases from the medium to a high congested level. For instance, the total freeway delay reduces from the medium level of 14,350 vehicle-minutes to the high level of 12,459 vehicle-minutes under the proposed model, compared to 15,997 vehicle-minutes and 20,552 vehicle-minutes if with TRANSYT-7F. These results seem to reflect the need to consider the impact of queue spillback on the freeway delay in design of interchange control strategies, and also to indicate the effectiveness of the proposed model that clearly outperforms TRANSYT-7F, one of the most powerful programs for arterial signal design but not including the off-ramp queue impact on the freeway.
Table 6-7 Total delay comparison by roadway segment (vehicle minutes)

<table>
<thead>
<tr>
<th>Demand Scenarios</th>
<th>Simulation Results from CORSIM (One hour)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ICIC</td>
</tr>
<tr>
<td>Low Freeway</td>
<td></td>
</tr>
<tr>
<td>I495IL</td>
<td>5219.0</td>
</tr>
<tr>
<td>I495OL</td>
<td>10807.5</td>
</tr>
<tr>
<td>Total</td>
<td>16312.2</td>
</tr>
<tr>
<td>Arterial</td>
<td></td>
</tr>
<tr>
<td>MD97NB</td>
<td>2795.9</td>
</tr>
<tr>
<td>MD97SB</td>
<td>7439.4</td>
</tr>
<tr>
<td>Total</td>
<td>16426.4</td>
</tr>
<tr>
<td>Medium Freeway</td>
<td></td>
</tr>
<tr>
<td>I495IL</td>
<td>5253.9</td>
</tr>
<tr>
<td>I495OL</td>
<td>8785.4</td>
</tr>
<tr>
<td>Total</td>
<td>14350.2</td>
</tr>
<tr>
<td>Arterial</td>
<td></td>
</tr>
<tr>
<td>MD97NB</td>
<td>3128.8</td>
</tr>
<tr>
<td>MD97SB</td>
<td>9176.8</td>
</tr>
<tr>
<td>Total</td>
<td>18220.1</td>
</tr>
<tr>
<td>High Freeway</td>
<td></td>
</tr>
<tr>
<td>I495IL</td>
<td>5333.8</td>
</tr>
<tr>
<td>I495OL</td>
<td>6787.1</td>
</tr>
<tr>
<td>Total</td>
<td>12459.7</td>
</tr>
<tr>
<td>Arterial</td>
<td></td>
</tr>
<tr>
<td>MD97NB</td>
<td>2558.9</td>
</tr>
<tr>
<td>MD97SB</td>
<td>6650.7</td>
</tr>
<tr>
<td>Total</td>
<td>14894.9</td>
</tr>
</tbody>
</table>

* Delay improvement = TRANSY7F Delay – The Proposed Model Delay
  Delay Improvement (%) = (TRANSY7F Delay – The Proposed Model Delay)/the Proposed Model
  Delay × 100%
  C.I. = confidence Interval

Freeway total delay comparison

Figure 6-4 and Figure 6-5 illustrates the relationship between the delay and the volume exiting from off-ramp H. Results from both figures and Table 6-7 indicate that the delay on I-495 Inner Loop (IL) is relatively stable as its traffic conditions are less likely to be impacted by the volume change at Ramp-H. In contrast, the total delay incurred on I-495 Outer Loop (OL) at the same total system demand level expectedly decreases with an increase in the off-ramp H volume, since the arterial signals have taken
the freeway delay into account in computing the green times for the increased flows, and the freeway segment experiences a reduced volume on the mainline but no impact by the off-ramp queue. This explains why the I-495 OL delays under TRANSYT-7F are about 20 to 30 percent higher than the proposed model.

![Figure 6-4 Comparison freeway delay by segment](image)

Arterial delays comparison

Considering the arterial delays illustrated in Figure 6-5, the integrated control model clearly outperforms TRNASYT-7F under the same local traffic demand but different off-ramp volumes. For instance, the total arterial delay under the proposed model during the medium Ramp-H volume was 18220.1 vehicle-minutes, far less than the total of 21672 vehicle-minutes if with the TRANSYT-7F model. The integrated model also demonstrates the same superior performance under the scenario of having a high Ramp-H volume (i.e., 14894 vehicle-minutes versus 21146 vehicle minutes).

Note that the integrated control model with its embedded formulations for queue spillback and lane blockage is able to significantly reduce the delay at congested
intersections, as evidenced by the resulting total delay in MD 97 SB that is a near-oversaturated segment during the peak commuting period (i.e., 4,538 vehicles per hour).

Figure 6-5 reflects an interesting relationship between the MD97 SB delay and the receiving volume at off-ramp-H, where its total delay increased from 7439 vehicle-minutes at the low off-ramp volume to 9176.8 vehicle-minutes at the medium off-ramp volume, and then reduced to 6650.7 vehicle-minutes when the off-ramp volume reached the high level. This pattern existed regardless of using the integrated model or TRANSYT-7F. It is due to the fact that both models are able to adjust the signal timing and cycle length to accommodate the increased volume from the increased off-ramp flows. For instance, the volume increase in MD97 SB from Intersection 2 to Intersection 4 demands an increase in their common cycle length and green split. The cycle lengths from the proposed model are 114 seconds, 142 seconds, and 164 seconds for low, medium, and high ramp volume, respectively. However, for drivers from all other intersection approaches, the increased volume on MD97 SB and the longer cycle length actually cause them to experience the higher total delay.

For MD 97 NB, the traffic volume stayed at the constant level, but its total delay exhibited an increase because of the reduced green time at signal 2 and the increased right-turn traffic from off-ramp H which generally result in an increased share of the total green duration.
6.5 Conclusion

This chapter presents the evaluation results of the integrated control models developed from this research with both field data from the interchange between I-495 and Georgia Avenue and the simulation experiments. The results of extensive experimental analyses clearly indicate that our proposed models with its embedded formulations to capture the traffic interactions between congested flow movements can yield effective signal control plans to prevent the formation of lane blockage and queue spillback during near oversaturated traffic conditions. In fact, the proposed models significantly outperform state-of-the-art signal model, TRANSYT-7F, with respect to all different MOEs at both moderate and congested volume levels, regardless of including the freeway segment delay due to the off-ramp queue in the control objection function or not. With the integrated interchange control model, potential users can decide the control objective based on the length of off-ramp queue spillback, and effectively mitigate the congestion level at all arterial intersections within the interchange impact boundaries.
CHAPTER 7: CONCLUSIONS AND RECOMMENDATIONS

7.1 Research findings

This study presented an integrated control system and its optimal computing models to contend with the impact of off-ramp queue spillback on both the freeway and arterials within the interchange control boundaries. The proposed system consists of two levels that compute the optimal coordinated signal strategies for intersections and off-ramps. Whereas the first level primarily handles oversaturated flows and blockage between lanes at congested intersections, the second level deals with the freeway mainline delays caused by the excessive off-ramp queue spillback; these components work together to produce the optimal systemwide signal and ramp control plan.

Since one or a few oversaturated intersection approaches on the congested arterial receiving freeway traffic could spill their queues either into neighboring lanes or back into their upstream intersections, the integrated model with its embedded formulations can redistribute the congestion among all intersections within the control boundaries, minimizing both the average and longest delays. Such a tool will allow responsible traffic agencies to design coordinated signal optimization plans for all intersections within an interchange’s impact boundaries and to decide if freeway delay should be included in the optimization process. Thus, the tool makes it possible to prevent freeway bottlenecks caused by off-ramp queues from propagating through upstream segments, consequently paralyzing the entire freeway network.

In addition to developing control modules for oversaturated arterials and excessive off-ramp queues, the study also conducted some experimental analyses using field data from the interchange at I-495 and Georgia Avenue. The remainder of this section summarizes some key research findings from the extensive numerical results:

– The interchange’s high off-ramp volume, in conjunction with the peak-hour arterial flow rates, will likely cause some intersection approaches to become oversaturated, consequently paralyzing traffic movements along the entire arterial.

– An oversaturated arterial adjacent to the interchange can cause different levels of congestion spillback at different intersection approaches; this oversaturation may
also cause off-ramp queue lengths to extend beyond their auxiliary lanes, blocking the freeway’s mainline lanes.

- State-of-the-art signal optimization programs, such as TRANSYT-7F, cannot yield effective signal control plans for oversaturated arterials that often experience lane blockage between neighboring lanes and queue spillback to their upstream segments.

- The integrated control model, with its embedded formulations — capable of capturing interactions between turning and through traffic flows, as well as congestion propagation between neighboring intersections — can effectively prevent the formation of local bottlenecks caused by queue spillback or lane blockage.

- This study shows that, by accounting for how off-ramp queues impact delays of both freeway and arterial traffic, the interchange system optimal control can yield the best use of a roadway’s overall capacity and prevent the formation of freeway queues in the interchange area caused by the overflow of off-ramp traffic.

- The integrated control model developed from this study can serve as an effective tool for responsible highway agencies to exercise the proper level of control based on the distribution of traffic volumes on freeway and arterials, as well as ramp queue lengths.

7.2 Recommendations for future studies

Building on the results of this study, we recommend that the following future tasks be conducted to effectively contend with the severe congestion patterns found around most urban freeway interchange areas:

- Extend the integrated interchange model to include coordinated on-ramp metering control, as on-ramp queues could spill back into the local arterial when freeway volume approaches or exceeds its capacity;

- Enhance the computing efficiency of the current GA-based solution to ensure its applicability to a real-time control environment;
Generalize the formulations for the existing control model to handle multiple interchanges — which will include one freeway segment, several parallel or connected arterials, and multiple on- and off- ramps — since freeway congestion caused by excessively long off-ramp queues could spill back to an upstream interchange during peak hours;

Develop a robust control algorithm capable of producing reasonably reliable results under the constraints of real-time data deficiencies, such as insufficient sensor information for input needs or measurement errors embedded in surveillance systems for computing the optimal control strategies;

Integrate with advanced travel information systems to guide the distribution of traffic during congested peak periods, and

Conduct field experiments to test the effectiveness of the proposed integrated control system under various real-world information constraints and uncertainty of driver responses to any implemented control strategies or guidance.
REFERENCES


122. Yuan, L. and J. Kreer "Adjustment of freeway ramp metering rates to balance entrance ramp queues."


